

**Excitable Cell Physiology -- Problem Set #1:**  
**Does the Migration of Ions from one Compartment to Another**  
**During the Establishment of a Donnan Equilibrium**  
**Significantly Affect Ionic Concentrations?**

**Review** the concept of capacitance before attempting this problem.

**Assume** that we have a very simple cell where the cation ( $C^+$ ) is the only diffusible species.

**Further** assume that the concentrations of  $C^+$  are:

$$[C^+]_{\text{inside}} = 0.1 \text{ M}$$

$$[C^+]_{\text{outside}} = 0.0019 \text{ M}$$

and the temperature is  $20^\circ \text{ C}$ .

1. Calculate the transmembrane potential for this system at equilibrium. (To make later calculations simple, round your answer to a whole number.)

2. The capacitance of a cell membrane is always normalized to area: it is expressed as farads/area. This is obviously necessary since bigger cells with bigger membranes would have larger capacitances (since capacitance is determined by the area of the conductors and the dielectric constant). **For a typical biological membrane, the capacitance is about:**

$$1 \text{ mF/cm}^2, \text{ i.e., } 10^{-6} \text{ Farads/cm}^2.$$

Recall that  $1 \text{ Farad} = \frac{\text{coulomb}}{\text{volt}}$

(a) Calculate the amount of charge stored across one  $\text{cm}^2$  of membrane when the cell is at Gibbs-Donnan equilibrium. Give your answer in coulombs per  $\text{cm}^2$ .

(b) Calculate the number of mols of  $C^+$  per  $\text{cm}^2$  of membrane. You will need the following constant:

1 Faraday of charge = 1 mol of univalent charged particles = 96,500 coulombs

(c) Now, assume that for this typical axon, we are concerned with a:

**1 cm ( $1 \times 10^{-2} \text{ m}$ ) long section with a diameter of 10  $\mu$  ( $10 \times 10^{-5} \text{ meters}$ ).**

Therefore, in this section, the axon has the following **surface area**:

$$= \text{length} \times \text{area} = L \times \text{diameter} \pi = 1 \times 10^{-2} \text{ m} \times \pi \times 1 \times 10^{-5} \text{ m}$$

$$= 3.142 \cdot 10^{-7} \text{ m}^2 = 3.142 \cdot 10^{-3} \text{ cm}^2$$

What is the number of charged particles stored in a membrane capacitor of this surface area?

(d) How many charged particles are present in the cytosol of this same bit of axon (1 cm with a 10 micron diameter)?

The internal concentration of  $C^+$  was given at the start as 0.1 M. We can calculate the volume as:

$$= \text{cross sectional area} * \text{length} = (\text{diameter}/2)^2 * \pi * L$$

$$= (5 * 10^{-5} \text{ m})^2 * \pi * 1 * 10^{-2} \text{ m} = 7.85 * 10^{-13} \text{ m}^3$$

and since  $1 \text{ cc} = 1 \text{ ml} = 10^{-6} \text{ m}^3$  then the volume is, in ml:

$$= 7.85 * 10^{-7} \text{ ml}$$

So, how many  $C^+$  particles reside in this tiny volume if the concentration of  $C^+$  is 0.1 M?

(e) What is the ratio of the number of charges separated in the establishment of the Gibbs-Donnan Equilibrium to the # number of ions still inside the cell?

(f) In the establishment of a Gibbs Donnan equilibrium, is there any meaningful change in the concentrations of the ions inside the cell?